# Exchange Reactions of Solid Oxides. Part III.* Magnesium Oxide. 

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#### Abstract

Exchange of ${ }^{18} \mathrm{O}$ between the surface of magnesium oxide and oxygen gas has been studied over the temperature range $370-510^{\circ}$, oxygen pressures of $1-14 \mathrm{~cm}$. being used. The rate of exchange and the amount of exchangeable oxide surface depend on the previous outgassing treatment of the oxide. The exchange process has an activation energy of approx. $3 \pm 2 \mathrm{kcal}$. mole ${ }^{-1}$ above 420-450 (depending on temperature of outgassing) and $34 \pm 2 \mathrm{kcal}$. mole ${ }^{-1}$ below this temperature. An alternative treatment of the kinetics gives $E$ for the high-temperature process of $7.7 \pm 2 \mathrm{kcals}$. mole ${ }^{-1}$ and for the lower temperature range approximately $36 \pm 2 \mathrm{kcal} . \mathrm{mole}^{-1}$. Rates of adsorption of oxygen by magnesium oxide at pressures near $10^{-3} \mathrm{~cm}$. show that at low pressures the initial adsorption has an activation energy of about $14 \mathrm{kcal} . \mathrm{mole}^{-1}$, but it is not possible with certainty to extrapolate to higher pressures and the nature of the rate-determining step in the two exchange processes remains uncertain.


Earlier papers (Houghton and Winter, Nature, 1949, 164, 1130; Winter, J., 1950, 1170; Winter, Discuss. Faraday Soc., 1950, 8, 231; Houghton and Winter, " Mass Spectrometry," Inst. of Petroleum, 1952, p. 127) have described the technique used to study the exchange of ${ }^{18} \mathrm{O}$ between enriched oxygen gas and finely-divided oxides: some discussion has also been given of the kinetics of the process. This paper reports a detailed investigation of the exchange with magnesium oxide : a study has been made of the effect upon the kinetics of varying the time and temperature of outgassing, the temperature of the exchange reaction, and the oxygen pressure. It must be emphasised that this work is concerned with the initial rapid exchange reaction, associated with the surface of the oxide (Houghton and Winter, Nature, loc. cit.). A few of these observations have been given elsewhere, and the earlier values for velocity constants in some cases differ slightly from those now quoted; this is due to a more careful evaluation of $\alpha_{0}$ and $\alpha_{\infty}$ (see idem, ibid.). In an attempt to identify the rate-determining step in the exchange, some measurements of the rate of adsorption of oxygen are reported here.

## Experimental

Materials.-Magnesium oxide was of "AnalaR" purity, made by igniting the carbonate in air at $800^{\circ}$ for $c a .4 \mathrm{hr}$. The oxygen, containing about $1 \cdot 2 \%$ of ${ }^{18} \mathrm{O}$, was prepared by electrolysis and was from the same stock as that used in earlier work; normal oxygen used for adsorption measurements was obtained by heating "AnalaR" potassium permanganate in vacuo; the first $10 \%$ of gas was rejected, and a middle fraction collected after passage through a trap cooled to $-78^{\circ}$. Helium used in the adsorption experiments was from the British Oxygen Company, spectroscopically pure, and was passed through a trap at $-78^{\circ}$ before use.

Results.-Experiments designed to show the effect of time and temperature of outgassing, and pressure of oxygen, $p_{0_{0}}$, in the reaction system, are summarised in Tables 1-3. It is evident that the rate of reaction at a fixed temperature is strongly dependent upon the first two variables, but is not very sensitive to $p_{0_{2}}$. In the later work these three conditions were kept approximately constant in order to study the effect of reaction temperature upon the rate constant, $k_{0}$, and the exchangeable surface oxygen, $n_{s}$ (atoms $/ \mathrm{g}$. of oxide). These experiments are summarised in Table 4 and Figs. 1 and 2, and yield the following rate equations, where $X$ and $X^{\prime}$ refer to the left-hand portion of the upper and the lower curve in Fig. 2 respectively and $Y$ and $Y^{\prime}$ to the right-hand portions.

$$
\begin{align*}
& X, k_{0}=0.15 \exp (-2400 / \boldsymbol{R} T)  \tag{1}\\
& Y, k_{0}=4.25 \times 10^{9} \exp (-35,400 / \boldsymbol{R} T)  \tag{2}\\
& X^{\prime}, k_{0}=0.12 \exp (-3000 / \boldsymbol{R} T)  \tag{3}\\
& Y^{\prime}, k_{0}=1.62 \times 10^{8} \exp (-33,000 / \boldsymbol{R} T)  \tag{4}\\
& * J ., 1950,1170,1175, \text { are regarded as Parts I and II. }
\end{align*}
$$

These equations are of the usual general form $k_{0}=A \exp (-E / \boldsymbol{R} T)$ : there is some uncertainty as to the exact values of $A$ and $E$, owing to the scatter of the results; the figures given above are the most probable values and the limits are given in Table 5.* This uncertainty is


Table 3. Dependence of $\mathrm{k}_{0}$ and $\mathrm{n}_{\mathrm{s}}$ upon $\mathrm{po}_{2}$.

| $\mathrm{PO}_{\mathrm{og}}$ (mm.) | Temp. |  | Outgassing time (hr.) | $k_{0}, \min .^{-1}$ | $n: \times 10^{-20}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }_{41}$ | $510^{\circ}$ | $491{ }^{\circ}$ | 14 | 0.0139 | 8.23 |
| 80 | 510 | 491 | 14 | 0.0160 | $8 \cdot 15$ |
| 83.5 | 510 | 493 | 14 | 0.0169 | 6.85 |
| 88 | 492 | 492 | 14 | 0.0149 | - |
| 147 | 492 | 492 | 14 | 0.0178 | - |
| 59 | 540 | 386 | 14, | $0 \cdot 0076$ | $3 \cdot 15$ |
| 11.7 | 540 | 386 | 14 | $0 \cdot 0069$ | $5 \cdot 15$ |
| 101.5 | 540 | 388 | 14 | 0.0065 | $3 \cdot 25$ |
| 11.5 | 540 | 450 | 14 | 0.0383 | $6 \cdot 30$ |
| 67.5 | 540 | 450 | 151 | $0 \cdot 0324$ | - |

regrettable but is due, we believe, to the extreme sensitivity of the oxide to the outgassing conditions; we were unable to control the temperature of the furnace to better than $\pm 5^{\circ}$ overnight. Recent work by Dr. J. A. Barnard upon zinc oxide (Thesis, London, 1952, and Part IV), which is more sensitive, has shown that by close control of the temperature (better than $\pm \frac{1^{\circ}}{}{ }^{\circ}$ overnight) the scatter of the $k_{\mathrm{n}}$ results is much reduced : it may be remarked, however, that the scatter of values of $n_{s}$ (cf. Fig. 1) is not removed.

To provide an alternative measure of surface, low-temperature ( $78^{\circ} \mathrm{K}$ ) nitrogen adsorption isotherms were measured for samples of the oxide which had been subjected to various outgassing treatments; these results are given in Table 6, calculated according to both the Harkins-Jura ( $J$. Chem. Phys., 1943, 11, 430) and the Brunauer-Emmett-Teller (B.E.T.) ( $J$. Amer. Chem. Soc., 1938, 60, 309) method. There is little difference between the surface areas given by the two theories, and we shall use the B.E.T. figures in discussion. Other results are given in Table 9.

[^0]TABLE 4. The effect of exchange reaction temperature on $\mathrm{k}_{0}$ and $\mathrm{n}_{\mathrm{s}}$ for magnesium oxide at constant outgassing temperature.

| $\begin{gathered} \mathrm{pog}_{\mathbf{2}} \\ (\mathrm{mm} .) \end{gathered}$ | Temp. |  | Outgassing | $\begin{gathered} k_{0,}, \\ \min .^{-1} \end{gathered}$ | $\stackrel{n_{s}}{\times 10^{-20}}$ | $\begin{gathered} \mathrm{Po}_{\mathbf{o}} \\ (\mathrm{mm} .) \end{gathered}$ | Temp. |  | Outgassing time | $\underset{\min .^{-1}}{k_{0}}$ | $\begin{aligned} & n_{s} \\ & \times 10^{-20} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Out- | xchange | time |  |  |  | Out- | Exchange |  |  |  |
|  | gassin | reaction | (hr.) |  |  |  | gassing | reaction |  |  |  |
| 76.6 | $510^{\circ}$ | $507{ }^{\circ}$ | 14 | 0.0194 | 10.6 | 67.9 | $540^{\circ}$ | $491^{\circ}$ | 16 | 0.0360 | $5 \cdot 35$ |
| 83.5 | 510 | 493 | $14{ }^{\prime}$ | 0.0169 | 6.85 | 76.9 | 540 | 475 | 18 | 0.0278 | 6.95 |
| $79 \cdot 7$ | 510 | 492 | 14 | 0.0160 | $8 \cdot 15$ | $72 \cdot 1$ | 540 | 462 | 13.5 | 0.0256 | 2.76 |
| $78 \cdot 4$ | 510 | 473 | 14 | 0.0150 | $7 \cdot 46$ | 69.0 | 540 | 459 | 17 | 0.0256 | 4.48 |
| 56.3 | 510 | 454 | 14 | 0.0159 | $5 \cdot 4$ | $67 \cdot 5$ | 540 | 450 | $15 \cdot 5$ | 0.0324 | 3.51 |
| $62 \cdot 1$ | 510 | 450 | 14 | 0.0163 | $5 \cdot 76$ | 74.9 | 540 | 442 | $14 \cdot 5$ | 0.0276 | $5 \cdot 91$ |
| $76 \cdot 2$ | 510 | 424 | 14 | 0.00804 | $5 \cdot 40$ | $78 \cdot 1$ | 540 | 419 | 13.5 | 0.0281 | $3 \cdot 15$ |
| $65 \cdot 0$ | 510 | 402 | 14 | 0.00347 | $5 \cdot 20$ | $78 \cdot 0$ | 540 | 403 | 14 | 0.0149 | $3 \cdot 72$ |
| $63 \cdot 2$ | 510 | 401 | 13.3 | 0.00293 | $3 \cdot 35$ | $56 \cdot 1$ | 540 | 397 | 14.5 | 0.0111 | $3 \cdot 70$ |
| $62 \cdot 1$ | 510 | 388 | 14 | 0.00215 | $4 \cdot 45$ | 59.3 | 540 | 386 | $14 \cdot 5$ | 0.00760 | 3-15 |
| $62 \cdot 4$ | 510 | 382 | 15 | 0.00148 | 6.26 | $100 \cdot 0$ | 540 | 382 | 13.5 | 0.00680 |  |
| $62 \cdot 6$ | 510 | 381 | 14 | 0.00132 | $5 \cdot 07$ | 61.6 | 540 | 368 | 14.5 | 0.00344 | 4•15 |
| $62 \cdot 2$ | 510 | 370 | $13 \cdot 8$ | 0.00112 | $5 \cdot 00$ |  |  |  |  |  |  |

Table 5. Accuracy of Arrhenius plots.

| Line | $A$ | $E$ | Line | $A$ | $E$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $X$ | $0.022-1.0$ | $2.4 \pm 2.8$ | $X^{\prime}$ | $0.036-0.42$ | $3.0 \pm 1.8$ |
| $Y$ | $(2.76-6.53) \times 10^{9}$ | $\mathbf{3 5 . 4} \pm 0.6$ | $Y^{\prime}$ | $3.2 \times 10^{7}-1.0 \times 10^{9}$ | $33.0 \pm 2.2$ |

Table 6. The surface areas of oxides by low-temperature nitrogen adsorption.

| Outgassing conditions |  | B.E.T.* |  | Harkins-Jura |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Time (hr.) | Temp. | C | $\mathrm{m} .2 / \mathrm{g}$. | A | m. ${ }^{2} \mathrm{~g}$. |
| 32 | $400^{\circ}$ | 22.5 | 62.3 | 282.3 | 68.2 |
| 48 | 400 | $27 \cdot 8$ | 62.0 | $283 \cdot 3$ | 68.3 |
| 64 | 400 | 29.4 | 61.5 | $260 \cdot 8$ | $65 \cdot 6$ |
| 16 | 500 | $29 \cdot 4$ | 61.5 | $260 \cdot 8$ | $65 \cdot 6$ |
| 14.5 | 835 | $44 \cdot 3$ | 21.8 | 33.96 | 23.7 |
|  | * The | nitro | le is ta | $16.2 \AA^{2}$ |  |

Table 7.
$p_{0}(\mathrm{~mm}$.
$\mathbf{7 6 \cdot 6}$
$\mathbf{8 7 . 7}$
$\mathbf{8 0 . 2}$
$\mathbf{8 6 . 4}$

| Outgassing conditions |  |
| :---: | :---: |
| Time (hr.) | Temp. |
| 18 | $540^{\circ}$ |
| 14 | 507 |
| 14 | 492 |
| 14 | 480 |
| 14 | 444 |


| Exchange reaction |  |
| :---: | :---: |
| temp. | $k_{0}, \min .^{-1}$ |
| $540^{\circ}$ | $0 \cdot 033{ }^{*}$ |
| 507 | 0.0194 |
| 492 | $0 \cdot 0149$ |
| 480 | $0 \cdot 00924$ |
| 444 | 0.00364 |

* Interpolated from Fig. 2.

Table 8. Oxygen adsorption rates.

| Expt. No. | $T$ | $10^{4} \times$ Initial oxygen pressure, cm . | $\left(\mathrm{d} n_{g} / \mathrm{d} t\right)_{t=0} \dagger$ | Expt. No. | $T$ | $10^{4} \times \text { Initial }$ <br> oxygen pressure, cm . | $t)_{s=0} \dagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Al | $432^{\circ}$ | $10 \cdot 8$ | $0 \cdot 30$ | A8 | $388^{\circ}$ | $10 \cdot 6$ | 0.19 |
| A3 | 484 | 9.8 | 0.73 | A9 | 416 | 11.2 | 0.24 |
| A4 | 470 | 11.0 | $0 \cdot 60$ | All | 412 | $10 \cdot 8$ | 0.23 |
| A5 | 386 | $10 \cdot 6$ | $0 \cdot 20$ | A2 * | 432 | 9.0 | $0 \cdot 45$ |
| A6 | 456 | $10 \cdot 5$ | 0.38 | A10 | 416 | 27.0 | $0 \cdot 42$ |
| A7 | 456 | 12.5 | 0.37 | Al2 | 486 | $20 \cdot 2$ | 1.05 |

* Run Al allowed to come to equilibrium ( 24 hr .), final pressure being $2.3 \times 10^{-5} \mathrm{~cm}$., and another dose of oxygen added; this gave an equilibrium pressure of $3.3 \times 10^{-5} \mathrm{~cm}$. after 24 hr .
$\dagger$ To convert to atoms min..$^{-1} \mathrm{~g} \mathrm{~A}^{-1}$ multiply by $3.07 \times 10^{16}$.
Table 9.

|  | Surface area, m..$^{2}$ g. $^{-1}$ |  |
| :---: | :---: | :---: |
| Outgassing | B.E.T. | Exchange |
| temp. | at $78^{\circ} \mathrm{K}$ | at $460^{\circ} \mathrm{C}$ |



|  | Surface area, m. ${ }^{2} \mathrm{~g} .^{-1}$ |  |
| :---: | :---: | :---: |
| Outgassing | B.E.T. | Exchange |
| temp. | at $788^{\circ}$ K | at $460^{\circ} \mathrm{c}$ |
| $600^{\circ}$ | $\mathbf{3 4 \cdot 4}$ | $\mathbf{4 0 . 0}$ |
| $\mathbf{5 4 0}$ | $\mathbf{3 8 \cdot 6}$ | $\mathbf{4 5 \cdot 3}$ |
| $\mathbf{5 1 0}$ | $\mathbf{6 1 . 5}$ | $\mathbf{6 9 . 7}$ |

Oxygen Adsorption Measurements.-The apparatus used was constructed from Pyrex glass and was of conventional design, comprising two McLeod gauges, covering the range $10^{-1}$ to $10^{-6} \mathrm{~mm}$. (all pressures are expressed in mm . of Hg ), a mercury manometer for measuring pressures above $10^{-1} \mathrm{~mm}$., a dosing system, and bulbs containing pure dry oxygen and helium. The adsorption vessel was of approximately the same size as that used for the exchange reactions: the apparatus was interconnected with taps lubricated with Apiezon vacuum grease, and was evacuated through a cold trap at $-78^{\circ}$ with a two-stage mercury diffusion pump backed by a rotary oil-pump. Dead-space determinations were made by using helium, and included measurements of the equivalent dead-space of the adsorption vessel, loaded with oxide, at all temperatures used. In the latter case the pressure of helium was adjusted to be approximately that of the oxygen at equilibrium in the adsorption measurements; the connecting tubing was of 7 mm . internal diameter, and it was established by calculation that under these conditions of measurement corrections due to possible thermal transpiration were negligible. Fresh lots of oxide were used for each experiment.

The procedure was to outgas the oxide sample (usually 1 g. ) overnight at $540^{\circ}$, as in the exchange experiments; if the vacuum in the morning was satisfactory ( $<10^{-5} \mathrm{~mm}$.) the oxide was isolated from the pumps and cooled to the desired temperature; when the temperature had been steady for about $20-30 \mathrm{~min}$. the adsorption was begun : if the morning pressure was too high the experiment was abandoned. Preliminary work showed that the amount of adsorption was very small, amounting to about $6-9 \times 10^{17}$ atoms $/ \mathrm{g}$., or about $0.1 \%$ of the exchangeable surface, at $485^{\circ}$, and 6 cm . upon 20 g . of magnesium oxide outgassed for 6 days to an ultimate pressure of $8 \times 10^{-6} \mathrm{~mm}$., at $535^{\circ}$ : this corresponds to a pressure drop in the system of about 0.1 cm . in 6 cm . : under these conditions the adsorption appeared complete in less than 10 min . A similar experiment at $388^{\circ}$ showed adsorption at 6 cm . pressure to be complete in, at the most, 5 min . It was, therefore, not possible to measure rates of adsorption at these pressures; such experiments were performed in the region of $10^{-2}-10^{-3} \mathrm{~mm}$. Observations were made at constant volume by expanding a known quantity of oxygen from the gas-dosing system into the adsorption volume and measuring the pressure on one or other of the McLeod gauges after suitable time intervals. Most adsorptions were followed to equilibrium, but the process obeyed unambiguously no simple law, and it was most convenient to evaluate ( $\left.\mathrm{d} n_{g} / \mathrm{d} t\right)_{t=0}$, the initial uptake rate ( $n_{g}$ in atoms/g. of oxide) : these figures are given in Table 8. From these results a plot of $\log \left[\left(\mathrm{d} n_{g} / \mathrm{d} t\right)_{t=0}\right]$ yields an apparent activation energy of about 13.8 kcal . mole ${ }^{-1}$. It is seen that in this pressure range the rate is roughly proportional to pressure (cf. expts. A3 and A12, and A9 and A10); also from expts. A1 and A2 the surface is not covered after the adsorption of $2.0 \times 10^{17}$ atoms $/ \mathrm{g}$., since at least a further $1.5 \times 10^{17}$ atoms $/ \mathrm{g}$. can be readily taken up at about the same pressure, in fact at an initial rate greater than that of the first adsorption on the freshly-outgassed oxide.

It is noteworthy that the rate of bombardment of the surface of 1 g . of oxide (taken as $62 \mathrm{~m} .{ }^{2}$ from the B.E.T. results of Table 6) at $456^{\circ}$ is about $8.6 \times 10^{25} \mathrm{molecules} / \mathrm{min}$. at a pressure of $10^{-3} \mathrm{~cm}$., according to simple kinetic gas theory: multiplication of this by the factor $\exp (-13,800 / R T)$ gives approximately $1.25 \times 10^{21}$ atoms per $g$. per min., which is roughly $10^{5}$ times the observed rate of adsorption at this temperature.

It was established that the rate of desorption from a partly-covered surface was slow. For instance, after the adsorption on 20 g . of oxide at 6 cm . pressure at $485^{\circ}$, the furnace temperature was raised to $540^{\circ}$, and the oxide evacuated for 15 min .; at the end of this time the pressure during pumping was $4 \times 10^{-3} \mathrm{~mm}$., and when the pumps were cut off the pressure rise in the adsorption system during 3 min . corresponded to a desorption rate of $3.4 \times 10^{15}$ atoms per g . per min. After a further 2 hours' pumping the corresponding figures were $6 \times 10^{-4} \mathrm{~mm}$. and $5.4 \times 10^{14}$ atoms per $g$. per min.

## Discussion

(a) Adsorption Studies.-It is interesting to compare the rates of exchange (at $\sim 6 \mathrm{~cm}$.) with those of adsorption (at $\sim 10^{-3} \mathrm{~cm}$.) at temperatures $456^{\circ}$ and $388^{\circ}$, which fall respectively in the regions of low and high activation energy for the exchange reaction. The initial rate of exchange, $v_{0}$, atoms per $g$. per min., may readily be shown to be given by

$$
v_{0}=n_{g} / w(-\mathrm{d} \alpha / \mathrm{d} t)_{t=0}=n_{a} k_{e} / w\left(\alpha_{0}-\alpha_{\infty}\right)
$$

where $k_{e}$ is the experimental first-order rate constant, $n_{g} / 2$ is the number of oxygen molecules in the gas phase, and $\alpha_{0}$ and $\alpha_{\infty}$ are the ${ }^{18} \mathrm{O}$ abundances of the gas respectively
at the beginning and the end of the reaction. The initial rate of adsorption, $v_{a}=$ $-\left(\mathrm{d} n_{g} / \mathrm{d} t\right)_{t-0}$ (cf. Table 8), and if this process is rate-determining, the maximum possible initial exchange rate would be $\left(\alpha_{0}-\beta_{0}\right) v_{a}$, where $\beta_{0}$ is the initial ${ }^{18} \mathrm{O}$ content of the oxide. For these two temperatures, with oxide outgassed at $540^{\circ}, v_{0}=1 \cdot 1 \times 10^{17},\left(\alpha_{0}-\beta_{0}\right) v_{a}=$ $1.1 \times 10^{14}\left(456^{\circ}\right)$, and $v_{0}=2.6 \times 10^{16},\left(\alpha_{0}-\beta_{0}\right) v_{a}=5.6 \times 10^{13}\left(388^{\circ}\right)$ atoms per g. per min. Since adsorption must precede exchange, we conclude that measurements of initial adsorption rates at low pressures on to an outgassed surface can tell us little about the rate-limiting factors in the exchange process at several cm . pressure. It may be remarked that at $388^{\circ}$, where adsorption (at 6 cm .) appeared complete in $<5 \mathrm{~min}$., the exchange, similar proportions of oxide and oxygen being used, had a time of half-change of 62 min .; the corresponding figures for $456^{\circ}$ were $<10$ and 17.3 min . However, the accuracy of these adsorption-rate measurements was low. It is unfortunately not possible to measure adsorption rates over a range of pressures from $10^{-3}$ to 6 cm . so as to determine the pressure dependence of the process, but assuming $v_{a} \propto p_{0}$, the values of $\left(\alpha_{0}-\beta_{0}\right) v_{a}$ become $3.4 \times 10^{17}$ $\left(388^{\circ}\right)$ and $6.6 \times 10^{17}\left(456^{\circ}\right)$, which are both greater than the corresponding $v_{0}$ figures.

It must be noted that the validity of a comparison of these figures with the values of $v_{0}$ given above is doubtful since, apart from the long extrapolation involved in assuming $v_{a} \propto p_{\mathrm{o}_{2}}$, the oxide surface is undoubtedly heterogeneous, as shown by the change of $n_{s}$ with temperature (cf. Table 4 and Fig. 1), and indicated also by the very low coverage ( $\sim 0.1 \%$ of the exchangeable surface, which is itself roughly equal to the B.E.T. area) at 6 cm . It is probably best to conclude that the adsorption studies do not allow us to reject either adsorption or desorption as possible rate-determining steps in the exchange process, although it is probable that adsorption is not the slow stage.
(b) Exchange Reaction.-Some discussion has been given elsewhere of the kinetics of this process (Houghton, Thesis, London, 1952; Houghton and Winter, op. cit.; Winter, loc. cit.), but some recapitulation and extension is convenient here, the notation of an earlier paper (Winter, Discuss. Faraday Soc., 1950, 8, 231) being used.

We may generalise the approach used there by assuming that the velocity of exchange, $v$ atoms min. ${ }^{-1}$, will be proportional to the product of a function $f\left(C_{g}\right)$ of the surface coverage with oxygen, and a function $\phi\left(n_{s}\right)$ of the exchangeable surface. Then

$$
\begin{align*}
v= & -n_{g}(\mathrm{~d} \alpha / \mathrm{d} t)=k_{e} n_{g}\left(\alpha-\alpha_{\infty}\right)  \tag{5}\\
& =w k_{\mathbf{1}}\left(C_{q}\right) \phi\left(n_{s}\right)(\alpha-\beta) \tag{6}
\end{align*}
$$

and remembering that the ${ }^{18} \mathrm{O}$ content of the reaction system remains constant,

$$
\begin{equation*}
\left(\alpha_{0}-\alpha_{\infty}\right) n_{g}=w n_{s}\left(\alpha_{\infty}-\beta_{0}\right) \tag{7}
\end{equation*}
$$

we have finally

$$
\begin{equation*}
k_{0} n_{s}=k_{1} \mathrm{f}\left(C_{g}\right) \phi\left(n_{s}\right)=n_{s} k_{e}\left[\left(\alpha_{\infty}-\beta_{0}\right) /\left(\alpha_{0}-\beta_{0}\right)\right] \tag{8}
\end{equation*}
$$

which may be compared with eqns. (2)-(11) of the paper given above.
It is thus seen that $k_{0} n_{s}$ may be a more important function than $k_{0}$; only when the term $\mathrm{f}\left(C_{g}\right) \phi\left(n_{s}\right)$ contains $n_{s}$ as a simple factor will it be correct to use $k_{0}$ : a brief discussion of some possible cases when the use of $k_{0}$ is justified has been given elsewhere (Winter, loc. cit.); a more detailed argument has been developed by Houghton (Thesis, London, 1952). In any case it must be remembered that neither $k_{0}$ nor $k_{0} n_{s}$ is likely to be identical with the true rate constant $k_{1}$, and activation energies calculated from the variation with temperature of these two functions will include the effect of temperature upon $f\left(C_{g}\right)$ and $\phi\left(n_{s}\right)$.

Possible rate-determining processes in the exchange are (a) adsorption of oxygen molecules, (b) dissociation of adsorbed molecules to ad-atoms, (c) diffusion of adsorbed atoms or molecules over the oxide surface, into surface cracks, pores, etc., (d) exchange proper, which must involve electron transfer between adsorbed oxygen and lattice oxygen or suitable lattice defects, (e) recombination of ad-atoms to molecules, ( $f$ ) desorption of oxygen molecules, and $(g)$ gaseous diffusion through the powdered oxide. Now processes (a) and $(f)$ involve only van der Waals forces; it has been established (Winter, unpublished work) that at liquid-oxygen temperatures physical adsorption and desorption of oxygen on
the magnesium oxide used in this study are rapid, being complete in less than a minute at oxygen pressures of $2-30 \mathrm{~cm}$. We can, therefore, eliminate these as possible ratedetermining steps at the much higher temperatures of the exchange reaction. We discard process (g) because exchange reactions in which the oxide was packed moderately firmly into a platinum boat gave the same rate constants as runs wherein the oxide was loosely spread over the bottom of the reaction vessel : this was confirmed for both slow and fast exchange rates. In addition, if $(g)$ were rate-determining, the temperature dependence of $k_{0}$ (or $k_{0} n_{s}$ ) should be that of the gaseous self-diffusion coefficient, i.e., proportional to $T^{n}$, where $0.5<n<1$; as noted above, the rate constants show an exponential dependence upon $T^{-1}$. A plot of $\log k_{0}$ or $\log k_{0} n_{s}$ against $\log T$ in the region of low $E$ gave a curve, from which it was obvious that $n \gg 1$. It is not possible to reject (c), particularly since, as we have already noted, the coverage at 6 cm . pressure is quite sparse. No unambiguous evidence upon this point was obtainable from the measurements of rates of adsorption of oxygen. It is, however, unlikely that the process of high activation energy is one of surface diffusion, although it is possible the high-temperature reaction, of low $E$,

Fig. 1.

$\times$ Outgassed at $510^{\circ} \mathrm{C} ; \mathrm{po}_{3}=6-8 \mathrm{~cm}$.
$\bigcirc$ Outgassed at $540^{\circ} \mathrm{C} ; p_{\mathrm{O}_{2}}=6-8 \mathrm{~cm}$.
Outgassed at $540^{\circ} \mathrm{c} ; \mathrm{poz}_{\mathrm{z}}=1 \cdot 1 \mathrm{~cm}$.

Fig. 2.

$\times$ Outgassed at $510^{\circ} \mathrm{c} ; \mathrm{poz}_{2}=6-8 \mathrm{~cm}$.
$\bigcirc$ Outgassed at $540^{\circ} \mathrm{c}$; $\mathrm{po}_{2}=6-8 \mathrm{~cm}$.

- Outgassed at $540^{\circ} \mathrm{c} ; p_{o_{2}}=1 \cdot 1 \mathrm{~cm}$.
is diffusion-controlled (cf. Tompkins, Trans. Faraday Soc., 1950, 46, 569; Patterson, ibid., 1953, 49, 802). Pending the completion of work now in progress, we postpone discussion of $(c)$, and are left with $(b),(d)$, and $(e)$ :

The experimental work presented here does not allow us to choose between ( $b-e$ ) and ( $d$ ) as rate-determining steps. If we assume, as seems reasonable, a rapid attainment of the steady state among the adsorbed species, reactions (b) and (e) become indistinguishable, and the apparent activation energy of the exchange reaction, when this is controlled by (b)(e), will, in the usual way, reflect the change with temperature of the equilibrium between $\mathrm{O}_{2}$ (ads.) and O (ads.). Thus, considering this case, if we assume the rate of dissociation is proportional to the stationary concentration of $\mathrm{O}_{2}$ (ads.) and that the equilibrium lies well to the right (as is very probable since the lifetime of $\mathrm{O}_{2}$ on the surface at these temperatures is likely to be much less than that of an oxygen atom), then

$$
\begin{equation*}
k_{(b)} C_{g \gamma}=k_{(e)} C_{g}{ }^{2}(1-\gamma)^{2} \tag{9}
\end{equation*}
$$

where $C_{g}$ is the total concentration of adsorbed oxygen (atoms and molecules) expressed as atoms $/ \mathrm{g}$. of oxide, and $k_{(b)}, k_{(e)}$, are the corresponding rate constants. We have already assumed $k_{(b)} \gg k_{(e)}$, so that the degree of association, $\gamma$, of the oxygen is small, and

$$
\begin{equation*}
k_{(b)} C_{g} \gamma \approx k_{(e)} C_{g}{ }^{2} \tag{10}
\end{equation*}
$$

Then it follows from eqn. (8) that

$$
\begin{equation*}
k_{(e)} C_{g}{ }^{2}=n_{s} k_{\mathbf{0}}=n_{s} k_{e}\left[\left(\alpha_{\infty}-\beta_{0}\right) /\left(\alpha_{0}-\beta_{0}\right)\right] \tag{ll}
\end{equation*}
$$

where $k_{e}$ is the experimental first-order rate constant of the exchange reaction. If we further assume $C_{g} \propto n_{s}$, then (11) reduces to

$$
\begin{equation*}
k_{(e)}{ }^{\prime} C_{g}=k_{0} \tag{12}
\end{equation*}
$$

For the case when $(d)$ is rate-determining, we have the result (Winter, loc. cit.)

$$
\begin{equation*}
k_{(d)} C_{g}=k_{0} \tag{13}
\end{equation*}
$$

Note that in the derivation of eqn. (13) no assumption is needed regarding the relation between $C_{g}$ and $n_{s}$.

We may note also that the exchangeable oxygen, $n_{s}$, in the oxide surface (in atoms/g. of oxide), is given by eqn. (7), thus

$$
\begin{equation*}
n_{s}=\left(n_{g} / w\right)\left(\alpha_{0}-\alpha_{\infty}\right) /\left(\alpha_{\infty}-\beta_{0}\right) \tag{14}
\end{equation*}
$$



The experimental figures are presented in Fig. 2 in terms of $k_{0}$, and in accordance with the above analysis there is clear evidence of two processes, the characteristics of which are shown in Table 5.

It may be noted that if $(b)-(e)$ is rate-determining and $C_{g}$ is not proportional to $n_{s}$, then $\log k_{0} n_{s}$ and not $\log k_{0}$ should be used in the Arrhenius plot; if this is done with the data of Table 4, Fig. 3 results, in which the distinction between the two outgassing temperatures disappears for the high-temperature process and its activation energy is now $7 \cdot 7 \pm 2 \mathrm{kcal}$. mole ${ }^{-1}$; the activation energy for the lower-temperature region is not much changed, being $37.6 \pm 2$ and $35.9 \pm 1 \mathrm{kcal}$. mole ${ }^{-1}$ for outgassing temperatures of $510^{\circ}$ and $540^{\circ}$, respectively.

There are a number of other interesting points arising from the above kinetic analysis : thus the rate constants are not very dependent upon the oxygen pressure (Table 3), which may mean that in spite of the sparse coverage of the surface, the active sites are effectively saturated at pressures of $\mathbf{l ~ c m}$. upwards; i.e., that $C_{g}$ is virtually independent of $p_{\mathrm{O}_{2}}$ above 1 cm . up to the highest pressure used, viz., 14.7 cm .

The figures recorded in Table 7 were obtained before the importance of standardising the outgassing temperature was realised; they indicate an apparent activation energy for $k_{0}$ of about $26.5 \mathrm{kcal} . / \mathrm{mole}^{-1}$. These experiments refer to temperatures at which the " true" activation energy, at constant outgassing temperature, is around $3 \mathrm{kcal} . \mathrm{mole}^{-1}$ (cf. Table 4 and Figs. 1 and 3); it is likely that the difference reflects mainly an increase in the number $\left(S_{c}\right)$ of reactive sites as the outgassing temperature is raised, thus we may write

$$
k_{0}=A \exp (-E / \boldsymbol{R} T)=S_{c} Z_{c} \exp (-E / \boldsymbol{R} T)
$$

where $A$ is the coefficient of intrinsic catalytic activity (cf. Schwab, $Z$. physikal. Chem., 1929, 5, B, 406; 1930, 9, B, 265 ; Trans. Faraday Soc., 1946, 42, 689; Balandin, Z. physikal. Chem., 1932, 19, B, 451 ; Eckell, Z. Elektrochem., 1933, 39, 859; Cremer, Z. physikal. Chem., 1929, 144, A, 231 ; Storch, J. Amer. Chem. Soc., 1935, 57, 1395 ; Huttig, Kolloid-Z., 1941, 98, 263, and papers there cited), $Z_{c}$ is the frequency factor for energy transfer between the reactant species, and $S_{c}$ is the number of active sites on the catalyst surface. If this type of behaviour is typical, it indicates the great difficulty of properly interpreting heterogeneous catalytic phenomena. It is unfortunate in this connection that the figures given in Table 5 and eqns. (1)-(4) are not sufficiently accurate to show whether the increase in rate with outgassing temperature at constant reaction temperature is due to a change in $A$ or in $E$. The values for $k_{0}$ at $\sim 460^{\circ}$ on samples outgassed at temperatures from $866^{\circ}$ to $510^{\circ}$ yield the Arrhenius equation $k_{0}=19 \cdot 1 \exp (-10,900 \pm 700 / R T)$, if it is assumed that $k_{0}$ properly refers to the high-temperature exchange reaction. Alternatively, if $k_{0} n_{s}$ should be used, it is seen from the last column of Table 2 that the product rises to a flat maximum between outgassing temperatures of $550^{\circ}$ and $750^{\circ}$, falling sharply at $866^{\circ}$. This is very similar to the effect found by Huttig ( $Z$. physikal. Chem., 1934, 171, 83 ; Z. anorg. Chem., 1935, 223, 241 ; Kolloid-Z., 1942, 98, 6, 263) for the decomposition of nitrous oxide on spinels heat-treated at various temperatures. The sharp drop in reactivity, expressed as $k_{0} n_{s}$, around $750^{\circ}\left(\sim 0.33 T_{m}\right)$ is in agreement with the conclusions (Bevan, Shelton, and Anderson, $J ., 1948,1728$ ) that surface defects become mobile between 0.3 and $0.5 T_{m}$, where $T_{m}$ is the m. p. of the solid: the commencement of sintering is shown clearly by the results in Table 2 and the B.E.T. figures in Table 9.

The complexity of even the present, at first sight simple, reaction is further demonstrated by the heterogeneity of the oxide surface-as in the change of $n_{s}$ with reaction temperature (Fig. 2) and with outgassing temperature (Table 2). The heterogeneity indicated in Fig. 2 may also be demonstrated and confirmed by allowing a sample to reach equilibrium with ${ }^{18} \mathrm{O}$-enriched oxygen at a relatively low temperature, say $380^{\circ}$, and then quickly raising the furnace temperature by some $30^{\circ}$, whereupon a rapid exchange occurs with more of the oxide surface and a new equilibrium ${ }^{18} \mathrm{O}$-content of the oxygen is established; this process may be repeated several times, but up to a reaction temperature of $507^{\circ}, n_{s}$ is not more than $7 \%$ of the total oxygen in the oxide.

A comparison between the surface areas obtained from the B.E.T. plots and the $n_{s}$ values obtained by exchange has been made by assuming that the surface of the magnesium oxide powder consists of a random distribution of the (111), (110), and (100) planes, then, a radius of $1 \cdot 4 \AA$ being used for the oxygen ion, the average area occupied by an oxygen ion is $10 \cdot 1 \AA^{2}$, and the surface area of the oxide is given in each case by $10 \cdot 1 n_{s} \times 10^{-20} \mathrm{~m} .{ }^{2} / \mathrm{g}$. Table 9 gives some typical results and shows that the two methods give comparable figures at outgassing temperatures of up to $640^{\circ}$, but diverge somewhat above this, until at $860^{\circ}$, when considerable sintering has occurred, the B.E.T. values are some 5-8 times those obtained from the exchange.

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[^0]:    * The method of least squares was applied to the results, giving equal weight to $T$ and $\log k_{0}$; the limits were obtained from the quadratic mean error (cf. Whittaker and Robinson, "The Calculus of Observations," Blackie, Glasgow, 1946, p. 246).

